

03/07/14 Agenda

- Warm Up
- Section 7.5 day 2 - Rational Exponents & Radicals
- Homework
 - Worksheet 7.5 - Rational Exponents & Radicals
(1 - 33 odds)

Warm Up - Homework out!



Put your name on a slip of paper.

Simplify:

$$4a \boxed{b^0} = 4a \cdot 1 \\ = 4a$$

$$\frac{\boxed{3^{-2}}}{n^1} \rightarrow \frac{1}{3^2 n} = \frac{1}{9n}$$

$$\frac{1}{\boxed{c^{-1}}} \cdot \frac{1 \cdot c^1}{1} \\ = c$$

$$\frac{6a^{-1}c^{-3}}{\boxed{d^0}=1} \\ = \frac{6a^{-1}c^{-3}}{1} = \frac{6}{ac^3}$$

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Section 7.5 day 2 - Rational Exponents & Radicals

Target 7A

March 7, 2014

Review:

$$a^m a^n = a^{m+n} \quad \frac{a^m}{a^n} = a^{m-n}$$

$$(a^m)^n = a^{mn} \quad \left(\frac{a}{b}\right)^m = \frac{a^m}{b^m}$$

$$(ab)^m = a^m b^m$$

$$a^0 = 1 \quad a^{-n} = \frac{1}{a^n} \quad \frac{1}{a^{-n}} = a^n$$

Definitions:

Radicals:

INDEX \swarrow \searrow RADICAL SIGN
 $\sqrt[n]{a}$ \nwarrow RADICAND

The index gives the 'degree' of the root.

For a cube root, the degree is 3

When no index is written, assume the index is 2.

This is usually called the SQUARE ROOT.

$$5^2 = 25 \quad \sqrt{25} = \sqrt{5 \cdot 5} = 5$$

$$25^{\frac{1}{2}} = 5 \quad \sqrt[2]{25} = 5$$

$$2\sqrt{25} = 25^{\frac{1}{2}} = 5$$

$$\sqrt[3]{8} = 8^{\frac{1}{3}}$$

$$625^{\frac{1}{4}} = \sqrt[4]{625}$$

There are 2 ways to simplify:

1.) $\sqrt[3]{125} = \sqrt[3]{5 \cdot 5 \cdot 5} = 5$

2.) $\sqrt[4]{16} = 16^{\frac{1}{4}} = (2 \cdot 2 \cdot 2 \cdot 2)^{\frac{1}{4}} = 2$

Section 7.5 day 2 - Rational Exponents & Radicals

Target 7A

March 7, 2014

You try:

$$\begin{array}{l} \sqrt[3]{27} = \sqrt[3]{3^3} = 3 \\ \begin{array}{c} \swarrow \searrow \\ 9 \cdot 3 \\ \swarrow \searrow \\ 3 \cdot 3 \end{array} \end{array} \quad \begin{array}{l} \sqrt[5]{32} = 2 \\ \begin{array}{c} \swarrow \searrow \\ 4 \quad 8 \\ \swarrow \searrow \quad \swarrow \searrow \\ (2) \cdot (2) \quad (2) \cdot 4 \\ \quad \quad \quad \swarrow \searrow \\ \quad \quad \quad (2) \cdot (2) \end{array} \end{array} \quad \begin{array}{l} \sqrt[3]{64} = 4 \\ \begin{array}{c} \swarrow \searrow \\ 4 \cdot 16 \\ \quad \quad \swarrow \searrow \\ \quad \quad 4 \cdot 4 \end{array} \end{array} \quad \begin{array}{l} \sqrt[2]{36} \\ \wedge \end{array}$$

$$\begin{array}{l} \sqrt{225} = \sqrt{5 \cdot 5 \cdot 3 \cdot 3} \\ \begin{array}{c} \swarrow \searrow \\ (5) \cdot 45 \\ \swarrow \searrow \\ (5) \cdot 9 \\ \swarrow \searrow \\ (3) \cdot (3) \end{array} \end{array} \quad \begin{array}{l} = \sqrt{5^2 \cdot 3^2} \\ \downarrow \quad \downarrow \\ 5 \cdot 3 \\ 3 \cdot 5 = 15 \end{array}$$

$$\sqrt{625}$$

Section 7.5 day 2 - Rational Exponents & Radicals

Target 7A

March 7, 2014

You can also write rational exponents like $\frac{2}{3}$ in radical form.

$$\begin{aligned} 8^{\frac{2}{3}} &= 8^{2 \cdot \frac{1}{3}} = (8^2)^{\frac{1}{3}} = \sqrt[3]{8^2} \\ &8^{\frac{1}{3} \cdot 2} = (8^{\frac{1}{3}})^2 = \left(\sqrt[3]{8}\right)^2 \end{aligned}$$

So: $a^{\frac{1}{n}} = \sqrt[n]{a}$

and

$$a^{\frac{m}{n}} = \sqrt[n]{a^m} = \left(\sqrt[n]{a}\right)^m$$

Re-write the following multiplication of radicals using exponents then simplify:

$$\sqrt{x} \cdot \sqrt{x} = x^{\frac{1}{2}} \cdot x^{\frac{1}{2}} = x^{\frac{1}{2} + \frac{1}{2}} = x^1 = x$$

$$\sqrt[4]{y} \cdot \sqrt[4]{y} \cdot \sqrt[4]{y} \cdot \sqrt[4]{y} = y$$

$$\sqrt[3]{5} \cdot \sqrt[3]{5} \cdot \sqrt[3]{5} = 5^{\frac{1}{3}} \cdot 5^{\frac{1}{3}} \cdot 5^{\frac{1}{3}} = 5^{\frac{1}{3} + \frac{1}{3} + \frac{1}{3}} = 5^1 = 5$$

Write each expression in radical form or exponential form, then simplify:

$$b^{\frac{5}{3}} = \sqrt[3]{b^5}$$

$$h^{\frac{2}{5}} = \sqrt[5]{h^2}$$

$$27^{\frac{4}{3}} = \sqrt[3]{27^4} = 3^4 = 81$$

$$(16b^2)^{\frac{3}{2}} = \sqrt{(16b^2)^3} = \sqrt{16^3 b^6} = 4 \cdot 4 \cdot 4 \cdot b \cdot b \cdot b$$

$$\sqrt[5]{a^7} = a^{\frac{7}{5}}$$

$$\sqrt[3]{8c^5} = 8^{\frac{1}{3}} c^{\frac{5}{3}} = 2c^{\frac{5}{3}}$$

$$(\sqrt{64})^3 = (64^{\frac{1}{2}})^3 = 64^{\frac{3}{2}}$$

$$b^{\frac{1}{3}} (ab)^{\frac{1}{2}} = b^{\frac{1}{3}} \cdot a^{\frac{1}{2}} \cdot b^{\frac{1}{2}} = a^{\frac{1}{2}} \cdot b^{\frac{1}{3} + \frac{1}{2}} = a^{\frac{1}{2}} \cdot b^{\frac{2}{6} + \frac{3}{6}} = a^{\frac{1}{2}} b^{\frac{5}{6}} = \sqrt[6]{a^3 b^5}$$

$$b^{\frac{5}{3}} = \sqrt[3]{b^5}$$